

Ch. 9 Properties of Transformations

9.1 Translate Figures and Use Vectors

- Translate: Slide
 - Preimage \longrightarrow image
 - Rule: $(x,y) \longrightarrow (x + a, y + b)$
 - $ABC \longrightarrow A'B'C'$
- **Isometry**: same length, same angles
 - Congruent transformation
- A translation is an isometry

- **Vectors:** used in a translation
 - Initial point and terminal point
 - Quantity that has both:
 - 1.) direction and 2.) magnitude (size)
 - Component: ⟨horizontal move, vertical move⟩

9.2 Matrices

- **Matrix:** rectangular arrangement of numbers
 - Matrices (plural)
 - A way to collect data (like x/y points)
 - Rows (across)
 - Columns (down)
 - Dimensions: row x column
 - Each number an element

- Add or Subtract Matrices: Each element
- Multiply: Each Row by Column, then add parts
 - Row elements must match column elements

9.3 Reflections

- Reflection: transformation
 - Uses a line like a mirror to reflect the image
 - Line of Reflection
- 4 Reflections:
 - 1. x-axis $(x,y) \longrightarrow (x, -y)$
 - 2. y-axis $(x,y) \longrightarrow (-x,y)$
 - 3. Line $y = x$ $(x,y) \longrightarrow (y,x)$
 - 4. Line $y = -x$ $(x,y) \longrightarrow (-y, -x)$

9.4 Perform Rotations

- **Transformations:**
 - 1. Translation (slide)
 - 2. Reflection (flip)
 - 3. Rotation (turn)
- **Rotation:** turn on a fixed point called the Center of rotation
Forms an Angle of rotation
Clockwise or Counterclockwise (we will use)

- Angle of Rotations: 90° , 180° , 270° , 360°
- 90° $(x,y) \longrightarrow (-y, x)$ or Matrix $\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$
- 180° $(x,y) \longrightarrow (-x,-y)$ or Matrix $\begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$
- 270° $(x,y) \longrightarrow (y, -x)$ or Matrix $\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$

9.5 Apply Compositions of Transformations

- **Glide:** 1. translation 2. reflection
- **Composition:** 2 or more transformations
- **Theorem: Reflections in Parallel Lines**
 - Reflect/ reflect again lines k and m
 - 1. PP' perpendicular to lines k and m
 - 2. $PP' = 2 \times$ distance between lines k and m

Theorem: Reflection in Intersecting Lines

reflect/ reflect again

lines k and m intersect

1. Angle $BB' = 2 \times$ the angle of k and m

9.6 Symmetry

- **1. Line of Symmetry** is the line of reflection
 - An image can have more than 1 line of symmetry
- **2. Rotational Symmetry:** image mapped onto itself by rotating 180° or less
 - Point of rotation: center of symmetry

9.7 Dilations

- **Transformations:**

- 1. Translation 2. Reflection 3. Rotation
- All keep congruency (isometry)

- 4. **Dilation:** transformation where original figure and new image are **Similar**

- $k = \text{scale factor} \quad \frac{CP'}{CP} = \frac{\text{distance new image}}{\text{distance old image}}$
- $0 < k < 1$ Reduction
- $k > 1$ Enlargement

- **Matrices: Scalar Multiplication**
 - Multiplication by a real number (scalar)

 - Dilation with Matrices
 - Multiplication by scale factor (which is the scalar)